

**WHAT IS CLAIMED IS:**

1. A linear method for performing head motion estimation from facial feature data, the method comprising the steps of:

obtaining first facial image and detecting a head in said first image;

detecting position of four points  $P$  of said first facial image where  $P = \{p_1, p_2, p_3, p_4\}$ , and  $p_k = (x_k, y_k)$ ;

obtaining a second facial image and detecting a head in said second image;

detecting position of four points  $P'$  of said second facial image where  $P' = \{p'_1, p'_2, p'_3, p'_4\}$  and  $p'_k = (x'_k, y'_k)$ ;

and,

determining the motion of the head represented by a rotation matrix  $R$  and translation vector  $T$  using said points  $P$  and  $P'$ .

2. The linear method of claim 1, wherein said four points  $P$  of said first facial image and four points  $P'$  of said second facial image include locations of outer corners of each eye and mouth of each respective first and second facial image.

3. The linear method of claim 1, wherein said head motion estimation is governed according to:

$$\mathbf{P}'_i = R\mathbf{P}_i + \mathbf{T}, \quad \text{where } R = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = [r_{ij}]_{3 \times 3} \quad \text{and } \mathbf{T} = [T_1 \ T_2 \ T_3]^T$$

represent camera rotation and translation respectively, said head pose estimation being a specific instance of head motion estimation.

4. The linear method of claim 3, wherein said head motion estimation is governed according to said rotation matrix  $R$ , said method further comprising the steps of:

determining rotation matrix  $R$  that maps points  $\mathbf{P}_k$  to  $\mathbf{F}_k$  for characterizing a head pose, said points  $\mathbf{F}_1, \mathbf{F}_2, \mathbf{F}_3, \mathbf{F}_4$  representing three-dimensional (3-D) coordinates of the respective four points of a reference, frontal view of said facial image, and  $\mathbf{P}_k$  is the three-dimensional (3-D) coordinates of an arbitrary point where  $\mathbf{P}_i = [X_i \ Y_i \ Z_i]^T$ , said mapping governed according to the relation:

$$\begin{aligned} R(\mathbf{P}_2 - \mathbf{P}_1) &\propto [1 \ 0 \ 0]^T \\ R(\mathbf{P}_6 - \mathbf{P}_5) &\propto [0 \ 1 \ 0]^T \end{aligned}$$

wherein  $\mathbf{P}_5$  and  $\mathbf{P}_6$  are midpoints of respective line segments connecting points  $\mathbf{P}_1\mathbf{P}_2$  and  $\mathbf{P}_3\mathbf{P}_4$  and, line segment connecting points  $\mathbf{P}_1\mathbf{P}_2$  is orthogonal to a line segment connecting points  $\mathbf{P}_5\mathbf{P}_6$ , and  $\propto$  indicates a proportionality factor.

5. The linear method of claim 4, wherein components  $r_1$ ,  $r_2$  and  $r_3$  are computed as:

$$\mathbf{r}_2^T (\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_3^T (\mathbf{P}_2 - \mathbf{P}_1) = 0$$

$$\mathbf{r}_1^T (\mathbf{P}_6 - \mathbf{P}_5) = 0$$

$$\mathbf{r}_3^T (\mathbf{P}_6 - \mathbf{P}_5) = 0$$

6. The linear method of claim 5, wherein components  $r_1$ ,  $r_2$  and  $r_3$  are computed as:

$$\mathbf{r}_3 = (\mathbf{P}_6 - \mathbf{P}_5) \times (\mathbf{P}_2 - \mathbf{P}_1),$$

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

7. The linear method of claim 4, wherein

$$\begin{bmatrix} \mathbf{P}_i^T & \mathbf{0}^T & \mathbf{0}^T & 1 & 0 & 0 \\ \mathbf{0}^T & \mathbf{P}_i^T & \mathbf{0}^T & 0 & 1 & 0 \\ \mathbf{0}^T & \mathbf{0}^T & \mathbf{P}_i^T & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_1 \\ \mathbf{r}_2 \\ \mathbf{r}_3 \\ \mathbf{T} \end{bmatrix} = \mathbf{P}_i',$$

each point pair yielding 3 equations, whereby at least four point pairs are necessary to linearly solve for said rotation and translation.

8. The linear method of claim 7, further comprising the step of: decomposing said rotation matrix  $R$  using Singular Value Decomposition (SVD) to obtain a form  $R = USV^T$ .

9. The linear method of claim 7, further comprising the step of computing a new rotation matrix according to  $R = UV^T$ .

10. A linear method for performing head motion estimation from facial feature data, the method comprising the steps of:

obtaining image position of four points  $P_k$  of a facial image;

determining a rotation matrix  $R$  that maps points  $P_k$  to  $F_k$  for characterizing a head pose, said points  $F_1, F_2, F_3, F_4$  representing three-dimensional (3-D) coordinates of the respective four points of a reference, frontal view of said facial image, and  $P_k$  is the three-dimensional (3-D) coordinates of an arbitrary point where  $P_i = [X_i \ Y_i \ Z_i]^T$ , said mapping governed according to the relation:

$$R(P_2 - P_1) \propto [1 \ 0 \ 0]^T$$

$$R(P_6 - P_5) \propto [0 \ 1 \ 0]^T$$

wherein  $P_5$  and  $P_6$  are midpoints of respective line segments connecting points  $P_1P_2$  and  $P_3P_4$  and, line segment connecting points  $P_1P_2$  is orthogonal to a line segment connecting points  $P_5P_6$ , and  $\propto$  indicates a proportionality factor.

11. The linear method of claim 10, wherein components  $r_1$ ,  $r_2$  and  $r_3$  are computed as:

$$r_2^T(P_2 - P_1) = 0$$

$$r_3^T(P_2 - P_1) = 0$$

$$r_1^T(P_6 - P_5) = 0$$

$$r_3^T(P_6 - P_5) = 0$$

12. The linear method of claim 11, wherein components  $r_1$ ,  $r_2$  and  $r_3$  are computed as:

$$\mathbf{r}_3 = (\mathbf{P}_6 - \mathbf{P}_5) \times (\mathbf{P}_2 - \mathbf{P}_1),$$

$$\mathbf{r}_2 = \mathbf{r}_3 \times (\mathbf{P}_2 - \mathbf{P}_1)$$

$$\mathbf{r}_1 = \mathbf{r}_2 \times \mathbf{r}_3$$

13. The linear method of claim 12, wherein a motion of head points is represented according to  $\mathbf{P}'_i = \mathbf{R}\mathbf{P}_i + \mathbf{T}$

where  $\mathbf{R} = \begin{bmatrix} \mathbf{r}_1^T \\ \mathbf{r}_2^T \\ \mathbf{r}_3^T \end{bmatrix} = [\mathbf{r}_{ij}]_{3 \times 3}$  represents image rotation,  $\mathbf{T} = [T_1 \ T_2 \ T_3]^T$

represents translation, and  $\mathbf{P}'_i$  denotes a 3-D image position of four points  $\mathbf{P}_k$  of another facial image.

14. The linear method of claim 13, wherein

$$\begin{bmatrix} \mathbf{P}_i^T & \mathbf{0}^T & \mathbf{0}^T & 1 & 0 & 0 \\ \mathbf{0}^T & \mathbf{P}_i^T & \mathbf{0}^T & 0 & 1 & 0 \\ \mathbf{0}^T & \mathbf{0}^T & \mathbf{P}_i^T & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{r}_1 \\ \mathbf{r}_2 \\ \mathbf{r}_3 \\ \mathbf{T} \end{bmatrix} = \mathbf{P}'_i,$$

each point pair yielding 3 equations, whereby at least four point pairs are necessary to linearly solve for said rotation and translation.

15. The linear method of claim 14, further comprising the step of: decomposing said rotation matrix  $\mathbf{R}$  using Singular Value Decomposition (SVD) to obtain a form  $\mathbf{R} = \mathbf{U}\mathbf{S}\mathbf{V}^T$ .

16. The linear method of claim 15, further comprising the step of computing a new rotation matrix according to  $R=UV^T$ .

17. A program storage device readable by machine, tangibly embodying a program of instructions executable by the machine to perform method steps for performing head motion estimation from facial feature data, the method steps comprising:

obtaining first facial image and detecting a head in said first image;

detecting position of four points  $P$  of said first facial image where  $P = \{p_1, p_2, p_3, p_4\}$ , and  $p_k = (x_k, y_k)$ ;

obtaining a second facial image and detecting a head in said second image;

detecting position of four points  $P'$  of said second facial image where  $P' = \{p'_1, p'_2, p'_3, p'_4\}$  and  $p'_k = (x'_k, y'_k)$ ;

and,

determining the motion of the head represented by a rotation matrix  $R$  and translation vector  $T$  using said points  $P$  and  $P'$ .

18. The program storage device readable by machine as claimed in claim 17, wherein said four points  $P$  of said first facial image and four points  $P'$  of said second facial image include locations of outer corners of each eye and mouth of each respective first and second facial image.

19. The program storage device readable by machine as claimed in claim 17, wherein said head motion estimation is governed according to:

$$P'_i = RP_i + T, \quad \text{where } R = \begin{bmatrix} r_1^T \\ r_2^T \\ r_3^T \end{bmatrix} = [r_{ij}]_{3 \times 3} \quad \text{and } T = [T_1 \ T_2 \ T_3]^T$$

represent camera rotation and translation respectively, said head pose estimation being a specific instance of head motion estimation.

20. The program storage device readable by machine as claimed in claim 19, wherein said head pose estimation is governed according to said rotation matrix  $R$ , said method further comprising the steps of:

determining rotation matrix  $R$  that maps points  $P_k$  to  $F_k$  for characterizing a head pose, said points  $F_1, F_2, F_3, F_4$  representing three-dimensional (3-D) coordinates of the respective four points of a reference, frontal view of said facial image, and  $P_k$  is the three-dimensional (3-D) coordinates of an arbitrary point where  $P_i = [X_i \ Y_i \ Z_i]^T$ , said mapping governed according to the relation:

$$R(P_2 - P_1) \propto [1 \ 0 \ 0]^T$$

$$R(P_6 - P_5) \propto [0 \ 1 \ 0]^T$$

wherein  $P_5$  and  $P_6$  are midpoints of respective line segments connecting points  $P_1P_2$  and  $P_3P_4$  and, line segment connecting points  $P_1P_2$  is orthogonal to a line segment connecting points  $P_5P_6$ , and  $\propto$  indicates a proportionality factor.